

Astronomy 210

Section 1 – MWF 1500-1550
134 Astronomy Building



This Class (Lecture 18):

Planetary Atmospheres

**HW 5 & Planetarium
due Friday!**

Next Class:

The Earth

Night Observations!

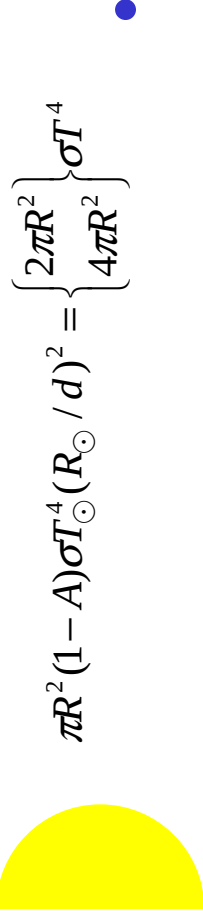
Astronomy 210 Spring 2005

Mar 2, 2005

Temperature



- Energy emitted per second is
 - $W_{\text{emit}} = S_{\text{emit}} \sigma T^4$
- In equilibrium:
 - $W_{\text{abs}} = W_{\text{emit}}$

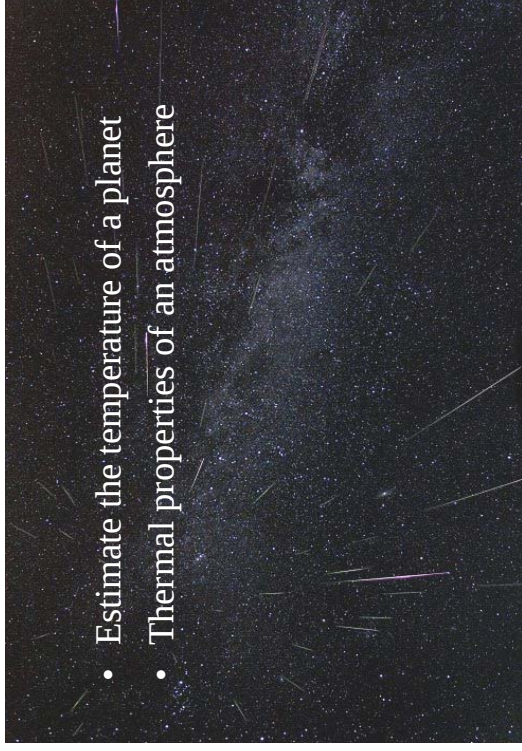


$$\pi R^2 (1 - A) \sigma T_{\odot}^4 (R_{\odot} / d)^2 = \left\{ \begin{array}{l} 2\pi R^2 \\ 4\pi R^2 \end{array} \right\} \sigma T^4$$

Astronomy 210 Spring 2005

Mar 2, 2005

Outline



- Estimate the temperature of a planet
- Thermal properties of an atmosphere

Astronomy 210 Spring 2005

Mar 2, 2005

Temperature



- Planet temperature set by star temperature!
- Does not depend on the planet's radius!



Where d is in AU!

Astronomy 210 Spring 2005

Mar 2, 2005

Temperature



- For Earth, we use $A = 0.37$, $d=1$ AU, fast rotator, night side and day side are similar temperature.

$$T = 279 \text{ K} \left(\frac{1-0.37}{1^2} \right)^{1/4} = 248.6 \text{ K}$$

$$T = -24 \text{ C} = -12 \text{ F}$$

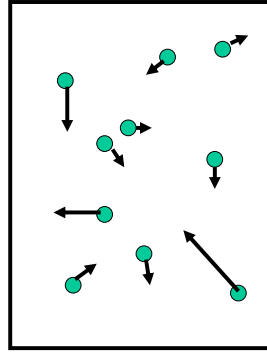
Okay, not a bad estimate. I didn't take into account the greenhouse effect, or the non-perfect blackbody modification. How would I do this for the Moon?

Atmosphere Models



"Particles in a box" gas model

- Particles move in random directions
- Particles "collide" and exchange kinetic energy
- Some particles move rapidly, others more slowly
- All are following a distribution of velocities



length of arrow
indicates speed of
molecule

Planetary Atmospheres

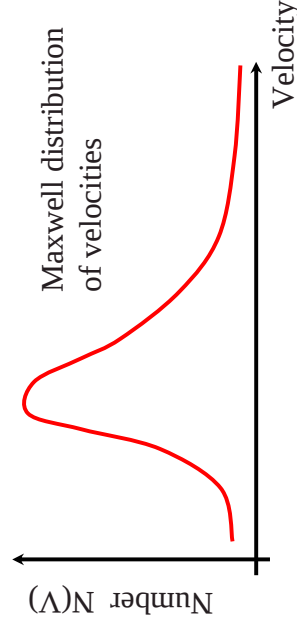


- **Atmosphere:**
 - The gaseous envelope surrounding a planet (or satellite)
- Terrestrial planets
 - Mercury + Moon: no substantial atmosphere
 - Venus + Mars: CO₂ rich atmospheres
 - Earth: N₂ + O₂ atmosphere
- Jovian planets
 - Molecular H and He atmospheres
- Titan: N₂ atmosphere

Distribution of Speeds



Looking at a large sample of particles produces a so-called Maxwell distribution of velocities.

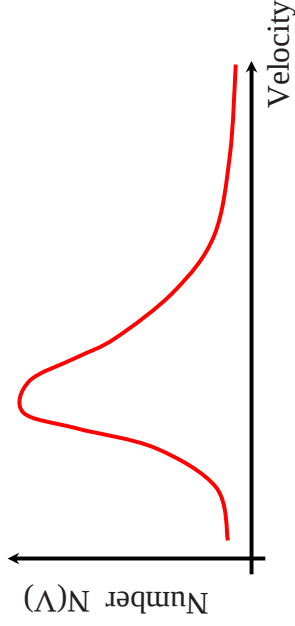


What is the average velocity?

Distribution of Speeds



Average velocity is defined as $\langle \vec{v} \rangle$



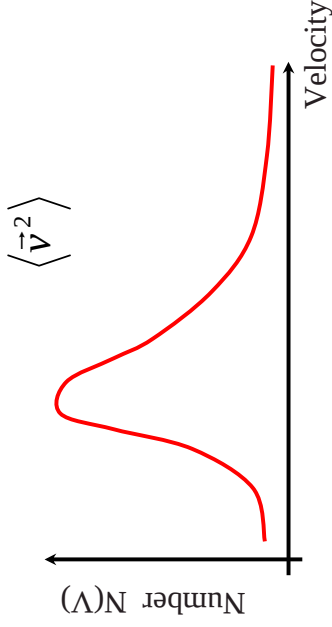
What is the average velocity?

Mar 2, 2005 Astronomy 210 Spring 2005

Distribution of Speeds



But what about average of the squared velocity?



What is the average squared velocity?

Mar 2, 2005 Astronomy 210 Spring 2005

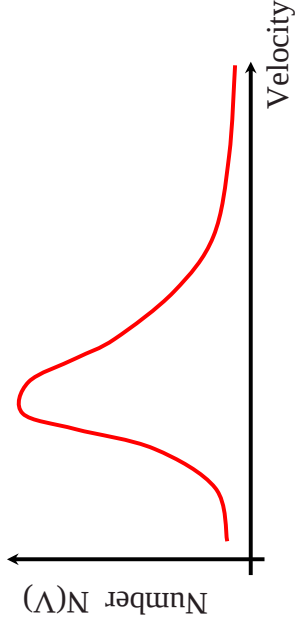
Distribution of Speeds



Boltzmann derived

$$\langle KE \rangle = \frac{1}{2} m \langle \vec{v}^2 \rangle = \frac{3}{2} kT$$

k is Boltzmann constant $1.38 \times 10^{-23} \text{J/K}$
m is the gas particle mass



Mar 2, 2005

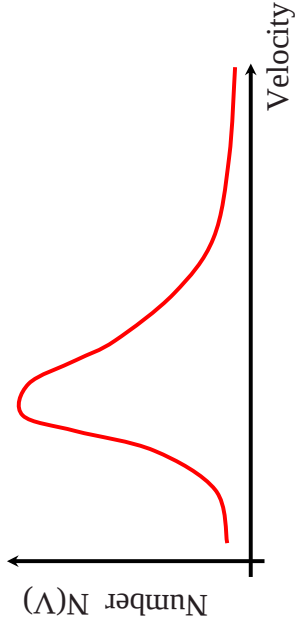
Astronomy 210 Spring 2005

Distribution of Speeds



Boltzmann derived

$$KE_{\text{peak}} = \frac{1}{2} m v_{\text{peak}}^2 = kT$$



Mar 2, 2005

Astronomy 210 Spring 2005

Temperature Results



- $V_{\text{rms}} \propto T \Rightarrow$ the hotter, the faster on average
- $V_{\text{rms}} \propto 1/m \Rightarrow$ the more massive, the slower on average
- In the classroom, the air is mostly N_2 ($\mu=28$) and O_2 ($\mu=32$), so Nitrogen is moving the fastest. How fast?
- At 300K (room temp), N is moving at an average velocity of 500 m/s!!! Or 1100 mph!
- Then what about smells?

Mar 2, 2005 Astronomy 210 Spring 2005

Planetary Atmospheres



- Terrestrial planets
 - No light gases (H_2 and He) only heavier N_2 , O_2 , CO_2
- Jovian planets
 - Mostly light gases (H_2 and He)

Why is there a difference?

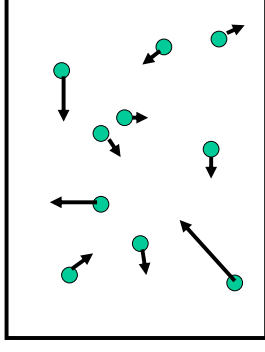
Mar 2, 2005 Astronomy 210 Spring 2005

Pressurized



Collisions with the walls of the box transfer momentum (change velocity) that implies a change in acceleration, which means a force. That force can be interpreted as pressure. For an ideal gas:

$$PV = NkT$$



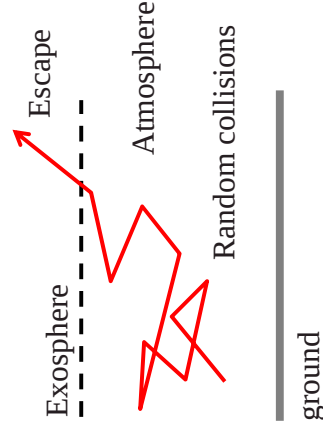
Mar 2, 2005 Astronomy 210 Spring 2005

Up, Up, and Away



- The atmosphere can escape!
- But what are the requirements?
- It is Gravity vs. Thermal Motion!

$$V_{\text{rms}} > V_{\text{escape}}$$



Analogy:
the atmosphere is
a gas in a leaky box

Mar 2, 2005 Astronomy 210 Spring 2005

Do I go or do I stay?



- Test case: H gas on the Moon.
- $$v_{\text{escape}} = \sqrt{2GM/R} = 2.4 \times 10^3 \text{ m/s}$$
- The average thermal speed for H on the Moon is
- $$v_{\text{rms}} = 2.6 \times 10^3 \text{ m/s}$$
- So $v_{\text{rms}} > v_{\text{escape}}$. Check, no H atmosphere on Moon!

Mar 2, 2005

Astronomy 210 Spring 2005

Not the Whole Story



- Even if $v_{\text{rms}} < v_{\text{escape}}$, some particles will still escape.
- Recall the ‘high-speed’ tail of the Maxwellian distribution
- For an object to keep an atmosphere over the age of the Solar System (4.5 billion years), the escape condition is more like



$$v_{\text{escape}} \geq 10 v_{\text{rms}}$$

This is a case of the tail wagging the dog

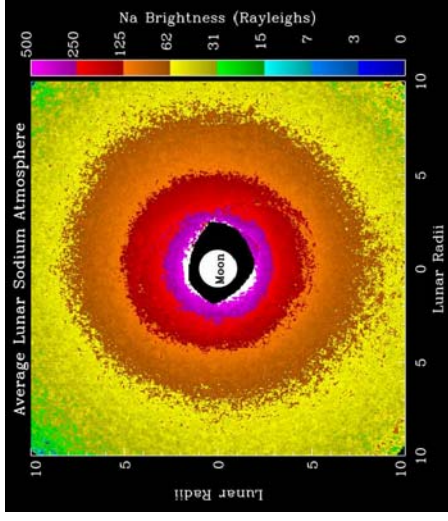
Mar 2, 2005

Astronomy 210 Spring 2005

Moon Atmosphere



- The Moon has a tenuous sodium atmosphere, that it is constantly losing and replenishing.
- Sort of like a comet in some ways.



Astronomy 210 Spring 2005

<http://sirlus.bu.edu/planetary/moon.html>

And?



Species	$v_{\text{escape}}/v_{\text{rms}}$	Lifetime
H on Moon	0.9	Hours
H on Earth	2.1	Days
Sodium on Moon	4	$\sim 10^3$ years
O ₂ on Earth	12	$\Rightarrow \infty$: no escape

Astronomy 210 Spring 2005

Mar 2, 2005

Earth's Atmosphere

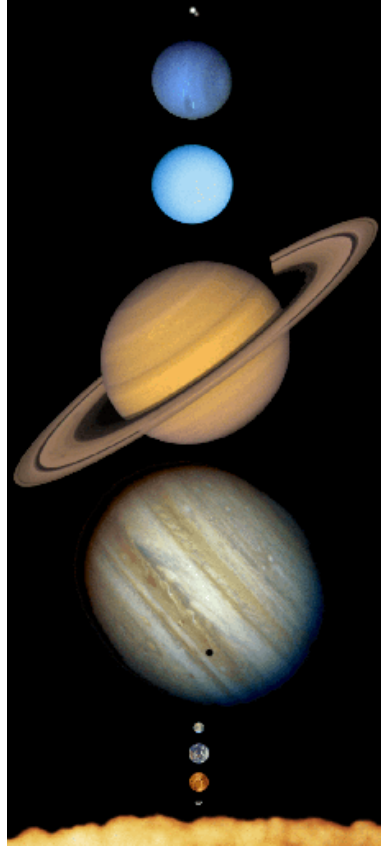


- Atmosphere is essential to live, made from Nitrogen and Oxygen– rare in other planets atmosphere
- However, this is the Earth's 3rd atmosphere
 - First was hydrogen and helium
 - Second was from volcanoes– carbon dioxide and some nitrogen (more like Venus)
 - Water helped dissolve the CO₂, and we arrived at the atmosphere we have today (thanks to life)

Mar 2, 2005

Astronomy 210 Spring 2005

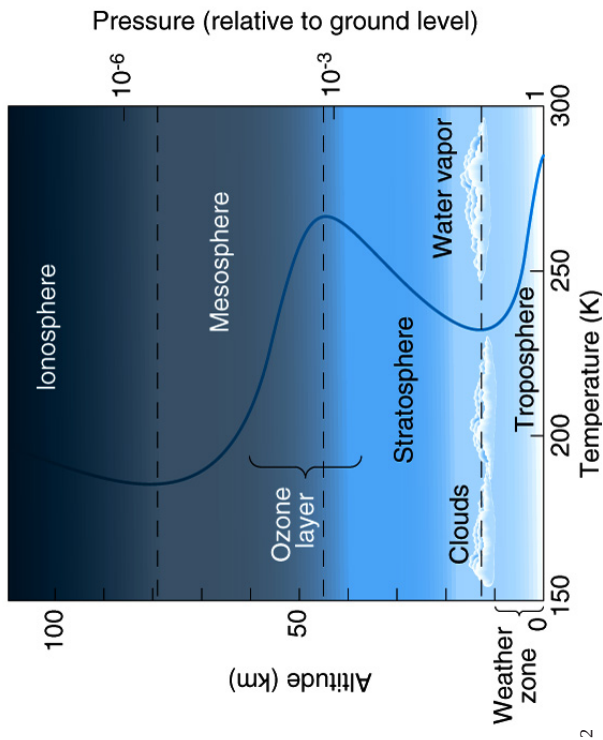
The Solar System is Ours!



Mar 2, 2005

Astronomy 210 Spring 2005

Layers of the Atmosphere



Mar 2